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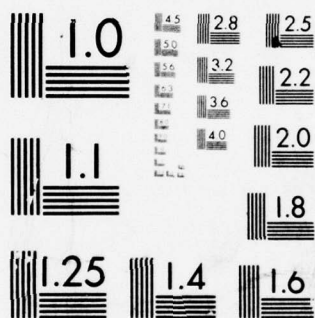UNCLASSIFIED   FTD-ID(RS)T-0900-77   NL

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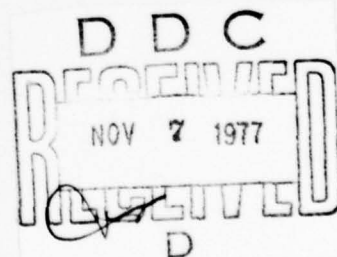# FOREIGN TECHNOLOGY DIVISION

THE CALCULATION OF INCLUSIVE GAMMA SPECTRA
AT HIGH ENERGIES

by

R. Blutner, S. Frank, et al.

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THE CALCULATION OF INCLUSIVE GAMMA SPECTRA AT HIGH ENERGIES [1]

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G. Ranft, J. Ranft and F. Thiel

1. Introduction

Gamma quanta which are produced in highly energetic pp
or πp collisions arise almost exclusively from the decomposition
of the π^0 mesons which are produced first:

$$
\begin{aligned}
\pi p &\rightarrow \pi^0 + \cdots \\
&\quad \llcorner\rightarrow \gamma + \gamma \\
pp &\rightarrow \pi^0 + \cdots \\
&\quad \llcorner\rightarrow \gamma + \gamma
\end{aligned}
\qquad (1)
$$

This fact makes it possible to find the differential effective
cross section of the γ quanta produced by purely kinematic
calculations from a known π^0 spectrum. The π^0 spectrum
is calculated according to the thermodynamic model [2, 4, 5,
6, 7, 9, 10]. This takes both of the essential possibilities
for production of π^0 mesons into consideration:

- The π^0 arises through direct decomposition of a fireball.
- The fireball is considered as a resonance. This resonance
  decomposes into π^0 and p.

In Section 2 we calculate, for the special case of isotropic

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(1) This work was produced under the care of Professors G. Ranft
and J. Ranft by a student group consisting of 7 second and
third year students (as part of the WPS), 2 graduates, one
research student and one aspirant. At the Exhibition of
The Karl Marx University, Leipzig, 1972, it was distinguished
with the Prize of the Karl Marx University, 1st Stage.

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π^0 spectra an expression for the differential effective cross section of the γ quanta.

For the general case of anisotropic π^0 distributions we give in Section 3 a Monte Carlo method with which the γ spectra can be calculated. In order to determine the γ spectra with good statistics, however, the Monte Carlo program requires a substantial computer time. Therefore, in Sections 4 (direct production of the π^0) and 5 (production of the π^0 through resonance) the spectrum is in part analytically calculated. Our results are reported in Section 6 and discussed in comparison with the existing experimental data.

2. The Calculation of γ-Spectra from Isotropic π^0 Spectra

Let an unstable particle of mass m be generated in a collision between particles a and b. Let the momentum spectrum of this particle be isotropic in the center of gravity system; that is,

$$\frac{d^3\sigma}{d^3\vec{p}} = \tilde{f}(|\vec{p}|) = \tilde{f}(p) = \tilde{f}(\varepsilon^2 - m^{*2}) = f(\varepsilon). \tag{2.1}$$

Let the particle of mass m decompose into particles 1* and j with masses m_1 and m_j. We seek the momentum spectrum $f_l(\varepsilon)$ of the particle 1 in the center of gravity system.

Under the assumption that the unstable particle disintegrates isotropically, $f_l(\varepsilon)$ can be determined from purely kinematic considerations. These calculations are presented in [3]. If, instead of the momentum distributions $f_l(\varepsilon)$ and $f(\varepsilon)$ one introduces the energy distributions

$$\omega(\varepsilon^*) = 4\pi p^* \varepsilon^* f(\varepsilon^*)$$
$$\omega_l(\varepsilon) = 4\pi p \varepsilon f_l(\varepsilon) \tag{2.2}$$

[Throughout the document 1 = Italic l.]

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then the result is

$$\omega_l(\varepsilon) = \frac{m^*}{2p_l} \int_{\varepsilon_-^*}^{\varepsilon_+^*} d\varepsilon^* \frac{\omega(\varepsilon^*)}{\sqrt{\varepsilon^{*2} - m^{*2}}} \qquad (2.3)$$

with

$$\varepsilon_\pm^* = \frac{m^*}{m_l^2} (\varepsilon\varepsilon_l \pm pp_l)$$

$$\varepsilon_l = \frac{m^{*2} + (m_l^2 - m_j^2)}{2m^*} \qquad (2.4)$$

$$p_l^2 = \varepsilon_l^2 - m_l^2 = \frac{[m^{*2} - (m_l + m_j)^2][m^{*2} - (m_l - m_j)^2]}{4m^{*2}}.$$

These relations, however, apply only if the rest masses of particles l and j are finite $(m_l \neq 0, m_j \neq 0)$.

On disintegration of the unstable particle of mass m into particles l and j with vanishing rest mass (e. g., γ quanta, a limit transition is necessary, $m_l = m_j = m \to 0$ This limit transition gives, for the limits, instead of the expression (2.4)

$$\varepsilon_-^* = \varepsilon + \frac{m^{*2}}{4\varepsilon} \; :$$

$$\varepsilon_+^* \to \infty. \qquad (2.5)$$

For finite collision energy, we must use instead of $\varepsilon_+^* \to \infty$ the maximum possible energy of the unstable particle:

$$\varepsilon_+^* = \varepsilon_{max}^*. \qquad (2.6)$$

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3. The Monte Carlo Procedure

If the momentum distribution of the unstable particle
of mass m is anisotropic, then (2.3) must be replaced by
a considerably more complex multiple integral which can be
evaluated only by means of drastic approximations (e. g., [11])
or tedious numerical calculations. In this case it is simpler
to calculate the γ spectrum using a Monte Carlo procedure.

In the Monte Carlo procedure the scattering or disin-
tegration process is simulated in a computer. Here we consider
the decomposition $\pi^0 \to 2\gamma$. The π^0 spectra can be specified
in arbitrary form (e. g., from an empirical formula, or
according to the thermodynamic model [2, 4, 5, 6, 7, 9, 10].
Corresponding to the selected statistics, from this one
determines the number of π^0 mesons which vanish in a single
phase space element. In the rest system of the π^0 the
disintegration $\pi^0 \to 2\gamma$ is isotropic (π^0 has zero spin). The
disintegration angle is a free parameter and in the Monte
Carlo procedure it is occupied by random numbers. Then the
disintegration is unambiguously defined. The momentum of the
γ quanta is transformed back to the starting system.
Corresponding to the phase space decomposition, the γ quanta
are assigned to their phase space elements. Thus one obtains
the γ distribution as a histogram.

4. γ Spectra According to the Thermodynamic Model; the
Contribution of Directly Generated π^0 Mesons

For the thermodynamic calculation of the contribution
to the γ spectra resulting from the disintegration of directly
generated π^0 mesons we need the function $f^0(\varepsilon, T)$. This
function designates the momentum distribution of the γ quanta
arising from directly generated π^0 mesons. Here, the reference
system for the resting system is a fireball of temperature T.

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According to the thermodynamic model [2, 4, 5, 7, 10] the spectrum of the directly generated π^0 mesons in the resting system of the fireball is isotropic:

$$f(\varepsilon^*) = \frac{z^* V}{8\pi^3} \cdot \frac{1}{e^{\varepsilon^*/T} - 1}. \tag{4.1}$$

In the following, we neglect the one in the denominator. If the π^0 disintegrates isotropically into particles of mass m_1 and m_j, then an elementary calculation of the integral (2.3) gives

$$f_i(\varepsilon) = \frac{m^* z^* z_1 V}{16\pi^3 p_1 p \varepsilon} T^2 \left[\left(1 + \frac{\varepsilon_-^*}{T}\right) e^{-(\varepsilon_-^*/T)} - \left(1 + \frac{\varepsilon_+^*}{T}\right) e^{-(\varepsilon_+^*/T)} \right] \cdot \quad \text{(cf. [3])} \tag{4.2}$$

Here m^* is the mass of the unstable particle (in our case, of the π^0 meson); z_1 and z^* are the multiplicities of the particles with masses m_1 and m^*, respectively. $f^0(\varepsilon, T)$ ε_-^*, ε_+^* and p_1 are given in Formula (2.4). The γ spectrum ∧ in the rest system of a fireball arises through the limit transition $m_i = m_j = m \rightarrow 0$.

As is shown in Section 2, in (4.2) we must use for ε_-^* and ε_+^* the expressions (2.5) and (2.6), respectively:

$$f_\gamma^0(\varepsilon, T) = \frac{z^* V}{8\pi^3 \varepsilon^2} T^2 \left[\left(1 + \frac{\varepsilon_-^*}{T}\right) e^{-(\varepsilon_-^*/T)} - \left(1 + \frac{\varepsilon_+^*}{T}\right) e^{-(\varepsilon_+^*/T)} \right]. \tag{4.3}$$

5. γ-Spectra According to the Thermodynamic Model; The Contribution of π^0 Mesons Generated by the Decomposition of Continuous Resonances

5.1 Formulation of the problem and transformation of the integral

We need the function $f^R(\varepsilon, T)$, which is the analog of the function $f^0(\varepsilon, T)$. But here the π^0 mesons are generated by the decomposition of a continuous resonance. Thus, we consider the disintegration scheme in (1). In order to obtain the

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momentum spectrum of the π^0 mesons from (4.2), we set there:

$$m_i = m_\pi$$
$$m_j = m_p \qquad\qquad (5.1)$$
$$m^* = \text{ mass of the resonance}$$

The momentum spectrum $f_\gamma^R(\varepsilon, T)$ of the γ quanta in the rest system of a fireball arises from this through a further integration of (2.3) and (2.4). Then we perform the limit transition $m_\gamma \to 0$:

$$f_\gamma^R(\varepsilon, T) = \frac{z_\gamma z_\pi z^* m^* V}{16\pi^3 p_\pi \varepsilon^2} T^2 \int_{\varepsilon_-}^{\varepsilon_+} \frac{d\omega}{\sqrt{\omega^2 - m_\pi^2}} \left[\left(1 + \frac{W_-}{T} \right) e^{-(W_-/T)} - \left(1 + \frac{W_+}{T} \right) e^{-(W_+/T)} \right] \quad (5.2)$$

$$\varepsilon_+ = \varepsilon_{max}$$
$$\varepsilon_- = \varepsilon + \frac{m_\pi^2}{4\varepsilon} = m\pi + \frac{1}{\varepsilon}\left(\varepsilon - \frac{m\pi}{2} \right)^2$$
$$W_\pm = \frac{m^*}{m_\pi^2} \left(\omega \varepsilon_\pi \pm \sqrt{\omega^2 - m_\pi^2} \sqrt{\varepsilon_\pi^2 - m_\pi^2} \right) \qquad\qquad (5.3)$$

$$\varepsilon_\pi = \frac{m^{*2} + m_\pi^2 - m_p^2}{2m^*}. \qquad\qquad (5.4)$$

Next, we must calculate the integral (5.2). We introduce the following designations:

$$I_\mp(\varepsilon) = \int_{\varepsilon_-}^{\varepsilon_+} \frac{d\omega}{\sqrt{\omega^2 - m_\pi^2}} \left(1 + \frac{W_\mp}{T} \right) e^{-(W_\mp/T)}. \qquad (5.5)$$

Because $\varepsilon_- \geq m_\pi$ and $\varepsilon_- = m_\pi$, only if $\varepsilon = m_\pi/2$, then for $\varepsilon \neq m_\pi/2$ the integrand in (5.5) is a continuous function in the range of integration. The substitution

$$\frac{\omega}{m_\pi} = \cos hz$$
$$\frac{\varepsilon_\pi}{m_\pi} = \cos ha \qquad\qquad (5.6)$$

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yields

$$I_{\mp} = \int_{z(\varepsilon_-)}^{z(\varepsilon_+)} dz \left[1 + \frac{m^*}{T} \cos h\,(z \mp a) \right] e^{-(m^*/T)\cos h\,(z \mp a)} .$$ (5.7)

A further substitution

$$I_- : \cos h\,(z - a) = y_-$$
$$I_+ : \cos h\,(z + a) = y_+$$ (5.8)

gives

$$I_{\mp} = \int_{y_{\mp}(\varepsilon_-)}^{y_{\mp}(\varepsilon_+)} \frac{1}{\sqrt{1 - (1/y^2)}} \left(\frac{m^*}{T} + \frac{1}{y} \right) e^{-(m^*/T)y}\, dy.$$ (5.9)

The function $y_{\pm}(\omega) = \cos h\,(z(\omega) \mp a)$ has the form

$$y_{\mp}(\omega) = \frac{\omega}{m_\pi} \frac{\varepsilon_\pi}{m_\pi} \mp \sqrt{\frac{\omega^2}{m_\pi^2} - 1} \sqrt{\frac{\varepsilon_\pi^2}{m_\pi^2} - 1}.$$ (5.10)

At the lower limit this expression simplifies to

$$y_-(\varepsilon_-) = \frac{\varepsilon}{m_\pi} v + \frac{m_\pi}{4\varepsilon} u \quad \text{falls} \quad \varepsilon > m_\pi/2$$

$$y_-(\varepsilon_-) = \frac{\varepsilon}{m_\pi} u + \frac{m_\pi}{4\varepsilon} v \quad \text{falls} \quad \varepsilon \leq m_\pi/2$$

$$y_+(\varepsilon_-) = \frac{\varepsilon}{m_\pi} u + \frac{m_\pi}{4\varepsilon} v \quad \text{falls} \quad \varepsilon > m_\pi/2$$ (5.11)

$$y_+(\varepsilon_-) = \frac{\varepsilon}{m_\pi} v + \frac{m_\pi}{4\varepsilon} u \quad \text{falls} \quad \varepsilon \leq m_\pi/2$$

at

$$v = \frac{\varepsilon_\pi}{m_\pi} - \sqrt{\left(\frac{\varepsilon_\pi}{m_\pi} \right)^2 - 1}$$

$$u = \frac{\varepsilon_\pi}{m_\pi} + \sqrt{\left(\frac{\varepsilon_\pi}{m_\pi} \right)^2 - 1}.$$ (5.12)

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We always have

$$y_{\mp}(\epsilon_-) \geq 1.$$

If $I(a,b)$ designates the integral (5.9) with the lower limit a and the upper limit b, then we must solve this integral for $\infty > b > a \geq 1$.

5.2 Analytical Solution

If the lower limit in (5.9) is large, then it is a good approximation to expand the root in the denominator as follows:

$$\left(1 - \frac{1}{y^2}\right)^{-1/2} \sim 1 + \frac{1}{2y^2}. \tag{5.13}$$

With this, (5.9) gives

$$I_A(a,b) = \int_a^b \left(\frac{m^*}{T} + \frac{1}{y} + \frac{m^*}{2Ty^2} + \frac{1}{2y^3}\right) e^{-(m^*/T)y}\, dy. \tag{5.14}$$

By virtue of the relations

$$\int_x^\infty \frac{e^{-(m^*/T)y}}{y}\, dy = -E_1\left(\frac{m^*}{T} x\right), \tag{5.15}$$

where $E_1(x)$ is the exponential integral and

$$\int \frac{e^{-(m^*/T)y}}{y^n}\, dy = \frac{1}{n-1}\left(-\frac{e^{-(m^*/T)y}}{y^{n-1}} - \frac{m^*}{T}\int \frac{e^{-(m^*/T)y}}{y^{n-1}}\, dy\right), \tag{5.16}$$

it is possible to calculate the integral (5.14):

$$I_A(a,b) = \left[e^{-(m^*/T)y}\left(1 + \frac{m^*}{4Ty} + \frac{1}{4y^2}\right) - E_1\left(\frac{m^*}{T} y\right)\left(\frac{m^{*2}}{4T^2} - 1\right)\right]_a^b. \tag{5.17}$$

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One can easily estimate that for a > 1.4 the error arising from the approximation (5.13) is less than 15%.

5.3 Numerical Solution

For a < 1.4 the approximation (5.13) cannot be used. In order to bring expression (5.9) into a suitable form for numerical calculations, we substitute here

$$y^2 - 1 = x^2$$

(5.18)

and obtain

$$I_N(a, b) = \int_{\sqrt{a^2-1}}^{\sqrt{b^2-1}} dx \left(\frac{m^*}{T} + \frac{1}{\sqrt{x^2 - 1}} \right) e^{-(m^*/T)\sqrt{1+x^2}}.$$

(5.19)

In order that the integrand not vary excessively, it is desirable to divide the term $(m^*/T)e^{-M^*/T(1 + (x^2/2))}$ additively:

$$I_N(a, b) = w(a, b) + II_N(a, b)$$

(5.20)

at

$$w(a, b) = \int_{\sqrt{a^2-1}}^{\sqrt{b^2-1}} dx \frac{m^*}{T} e^{-(m^*/T)(1 + (x^2/2))} = \sqrt{\frac{\pi}{2}} \sqrt{\frac{m^*}{T}} e^{-(m^*/T)} \left[\mathrm{erf.} \left(\sqrt{\frac{m^*}{T}} x \right) \right]_{\sqrt{a^2-1}}^{\sqrt{b^2-1}}$$

$$II_N(a, b) = \int_{\sqrt{a^2-1}}^{\sqrt{b^2-1}} dx$$

$$\times \left[\frac{m^*}{T} (e^{-(m^*/T)\sqrt{1+x^2}} - e^{-(m^*/T)(1 + (x^2/2))}) + \frac{1}{\sqrt{x^2 + 1}} e^{-(m^*/T)\sqrt{1+x^2}} \right].$$

(5.22)

Here $(z) = \dfrac{2}{\sqrt{\pi}} \displaystyle\int_0^z e^{-t^2} dt$ is the error function. The main part of w(a,b) appears in (5.20) if a and b are near 1.

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5.4   Summary

In the calculation of the γ spectrum in the rest system of the fireball (5.2) the integral (5.9)

$$I_- (y_-(\varepsilon_-), y_-(\varepsilon_+)) \quad \text{and} \quad I_+ (y_+(\varepsilon_-), y_+(\varepsilon_+))$$

must be solved. Depending on the positions of the lower limit, a, and the upper limit, b, we can distinguish 3 cases:

Case 1: $1.4 \approx uu \leq a < b$

Formula (5.17) is used with an error less than 15%.

Case 2. $1 \leq a < b \leq uu = 1.4$

(5.20) is used. $II_N (a, b)$ (5.22) here must be calculated numerically using a Gaussian integration formula.

If the upper integration limit here is far above the lower, then one can arbitrarily reduce the upper limit without making a large error. But the error occurring in the numerical integration is smaller.

Let us calculate

a) $m^*/T (b - a) < D$ (D specified ≈ 4)
$$I_N (a, b) = w (a, b) + II_N (a, b) \tag{5.23}$$
b) $m^*/T (b - a) > D$

Set $b = T/m^* D + a$ and calculate

$$I_N (a, b) = w (a, b) + II_N (a, b). \tag{5.24}$$

The error remains smaller than $e^{-D} \cdot 100\%$.

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Case 3. $1 \leq a \leq uu = 1.4 \leq b$

This case is reduced to cases 1 and 2:

$$J(a, b) = I_N(a, uu) + I_N(uu, b) \qquad (5.25)$$

The function (5.2) $f_\gamma^R(\varepsilon, T)$ for π^0 generated by resonance disintegration is computed numerically using the formulas above by means of a FORTRAN program. Using the program SPUK [9] a contribution to the differential effective cross section for γ production is calculated from this. The other contribution arises from the function $f_\gamma^0(\varepsilon, T)$ (Formula (4.3)). Both contributions, added, give the differential momentum spectrum for γ production.

6.   Results and Discussion

The version of the thermodynamic model based on the "strong bootstrap solution" (see [6]) is used for the thermodynamic calculation of the γ spectra. The free parameters of the model are adapted to 19 to 70 GeV/c data from pp collisions. We assume that the observed γ spectra can be completely explained from the decomposition of π^0 mesons. Our results indicate that this assumption is apparently justified. The thermodynamic parameters for the reaction $p + p \to \pi^0 + \cdots$ are needed for the calculation of the γ spectra. As there are neither thermodynamic calculations nor experimental data for this reaction, we use in place of the π^0 spectra the thermodynamic π^+ or π^- spectra. In Figure 1, the γ spectra calculated with the Monte Carlo procedure (Section 3) in the form $\delta^2 N/\delta p d\Omega$ in the center of gravity system are compared with the experimental data [1] for the reaction $p + p \to \gamma + \cdots$ at 23.1 GeV. For the calculation of the thermodynamic γ spectra

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it is assumed that the π^c spectra are identical with the π^+ spectra. Figure 2 shows the comparison of the same data with the direct thermodynamic calculation which was described in Sections 4 and 5. Here it was assumed that the π^0 spectra are identical with the π^- spectra.
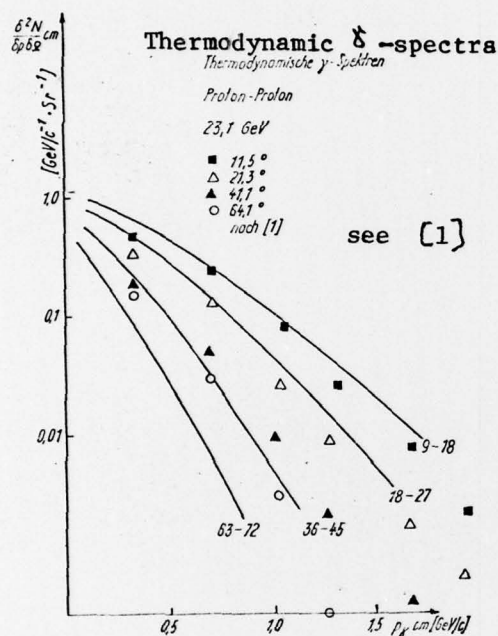

Figure 1. Comparison of the experimental γ spectra [1] in the form $(\partial^2 N/\partial p \partial \Omega)$ cm at $p_{lab} = 23{,}1$ GeV/c with the thermodynamically calculated γ spectra. The Monte Carlo method was used for the calculation. We used π^+ spectra instead of the π^0 spectra.
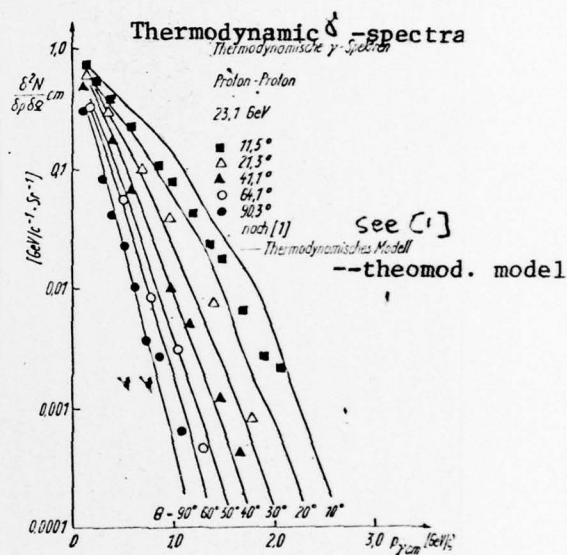
Figure 2. Comparison of the experimental γ spectra [1] in the form $(\partial^2 N/\partial p \partial \Omega)$ cm at $p_{lab} = 23{,}1$ GeV/c with the thermodynamically calculated γ Spectra. The analytical method was used for the calculation. We used π^- spectra instead of the π^0 spectra.

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Inclusive γ spectra $p + p \to \gamma + \cdots$ were measured in an ISR experiment [8]. The collision energy corresponded to laboratory momenta of up to 1,500 GeV/c. Figures 3 and 4 show the comparison of these data in the form $\partial^2 N/\partial p \partial \Omega$ in the center of gravity system with the analytically calculated γ spectra. It is likewise assumed that the π^0 spectra are identical with the π^- spectra. In Figure 5, one of the measured curves at $E_{cm} = 52.7$ GeV is compared with the result of the Monte Carlo method; as in Figure 1 the π^0 spectra are assumed to be identical with the π^+ spectra. In Figure 6, the data at $E_{cm} = 52.7$ GeV in the form $E(d^3 N/d^3 p)$ at $p_\parallel = 0$ are compared with the results of the Monte Carlo calculation.

We could establish that both methods for calculating the inclusive γ spectra according to the thermodynamic model yield consistent results, as can be seen from the calculated spectra at 23.1 GeV in Figures 1 and 2, and at 1,500 GeV in Figures 4 and 5. We find that the experimental data at 23.1 GeV approximately coincide with the calculated values. The deviations may be explained from the fact that we used the thermodynamic π^- or π^+ spectra instead of the π^0 spectra. At large angles, the major contribution to the spectra comes from the directly produced π^0 (Section 4). At smaller angles the contribution from π^0 produced in continuous resonances, calculated in Section 5, increases.

The thermodynamic calculation of the γ spectra at 1,000 and 1,500 GeV and the comparison with the ISR data is significant for the following reasons:

- Conclusions about the π^0 spectra at these high energies can be drawn from the γ spectra.
- The γ spectra are measured up to angles of 90° in the center of gravity system. The model is compared with experimental data for the first time at energies up to 1,500 GeV in the central region.
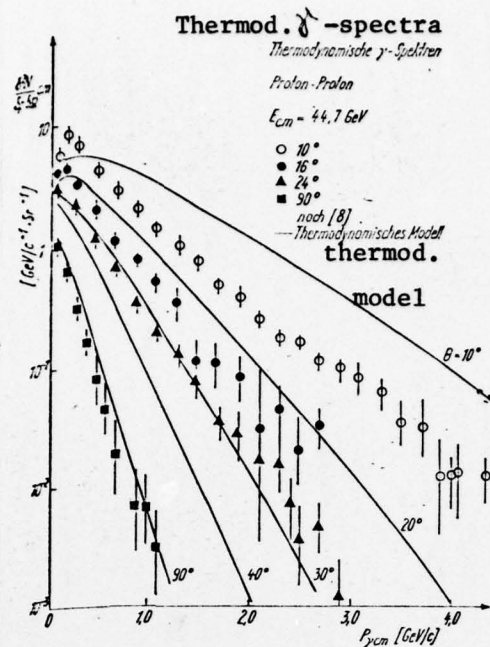
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Figure 3.   Comparison of the γ spectra measured by ISR [8] in the form $(\partial^2 N/\partial p\partial\Omega)$ cm at E_{cm} = 44.7 GeV with the thermodynamically calculated γ spectra. The analytical method was used for the calculation. We used π^- spectra instead of the π^0 spectra.
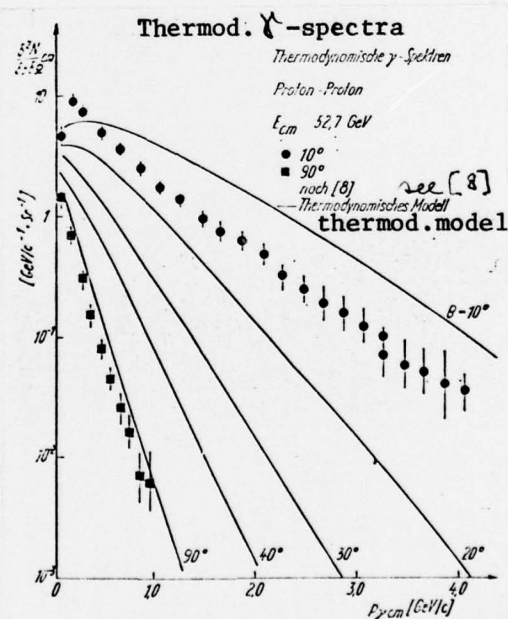

Figure 4.   Comparison of the inclusive γ spectra measured by ISR [8] in the form $(\partial^2 N/\partial p\partial\Omega)$ at E_{cm} = 52.7 GeV for a scattering angle of $\Theta_{cm} = 10, 2°, 90°$ with the thermodynamically calculated γ spectra. The analytical method was used for the calculation. We used π^- instead of the π^0 spectra.
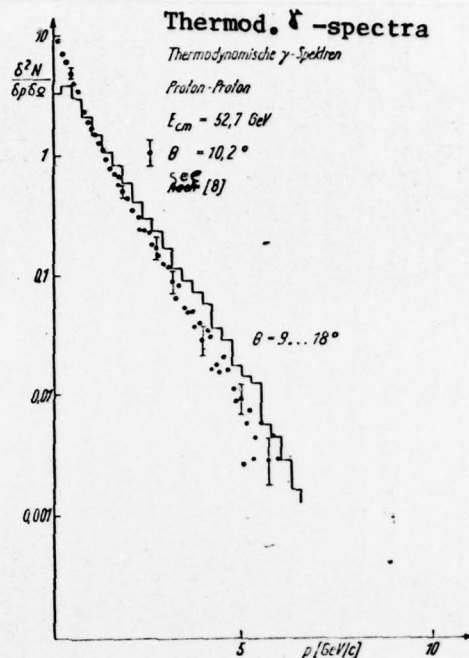
Figure 5. Comparison of the inclusive γ spectra [8] measured by ISR in the form $(\partial^2 N/\partial p \partial \Omega)$ for $\Theta = 10.2°$ at an energy E_{cm} = 52.7 GeV with the thermodynamically calculated γ spectra. The Monte Carlo method was used for the calculation. We used π^+ spectra instead of the π^0 spectra.
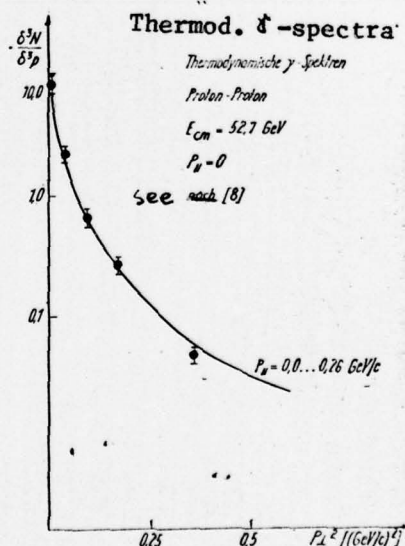

Figure 6. Comparison of the inclusive γ spectra [8] measured by ISR in the form $E \cdot (d^3 N/d^3 p)$ as a function of $p_\perp^2$ for $p_{||} \sim 0$ at an energy of E_{cm} = 52.7 GeV with the thermodynamically calculated γ spectra. The Monte Carlo method was used for the calculation. We used π^+ instead of π spectra.

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-    The thermodynamic π^+ and π^- spectra are compared at energies of 19 to 70 GeV with the data. It is shown in [6] that, for small angles and energies of 500 to 1,500 GeV, the extrapolated thermodynamic spectra, including their absolute standardization, approximately agree with the ISR data for inclusive π^+ or π^- production. In our work, likewise, the γ spectra, including their absolute standardization, are predicted in the entire kinematically possible range and compared with experimental data in a significantly larger angular range than in the case of the π^+ spectra.

Figures 3 to 6 show approximate agreement with the experiment. It follows from the agreement obtained that for these energies and the angles considered the differences between the π^+-, π^- and π^0 spectra are apparently slight. The thermodynamic spectra show "scaling" behavior and a non-vanishing central plateau [6]. It follows from the comparison with the γ data that the π^0 spectra in the fragmentation and pionization region apparently also show at least approximate "scaling" behavior. The deviations which occur between the thermodynamic γ spectra and the experiment we explain by the following facts:

1.   Use of π^+ or π^- spectra instead of π^0 spectra.
2.   Extrapolation of the thermodynamic spectra from lower energies or small angles to energies of 1,500 GeV and the entire angular range also, in the case of the π^+ and π^- spectra [6] leads to differences of the same order of magnitude from the experimental ISR data. Exact matching of the spectra with the ISR energies was not attempted in any of the cases.

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least, we thank Mrs. Eichel for the carefully performed
copy of the manuscript.

Summary

In high-energy collisions, γ quanta arise from the
disintegration of primarily produced π^0 mesons. The inclusive
momentum distributions of the γ spectra are computed through
a transformation of the π^0 spectra by means of the thermo-
dynamic model. The work was stimulated by a group of
Soviet physicists at the VIK Dubna, who performed the
corresponding experiment using a propane bubble chamber at
the 76 GeV accelerator at Serpuchow. The results of this
experiment should be used for comparison.

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